

UNIVERSITY OF NORTH BENGAL

B.Sc. Programme 1st Semester Examination, 2021

DSC1/2/3-P1-STATISTICS

DESCRIPTIVE STATISTICS

Time Allotted: 2 Hours

Full Marks: 40

 $1 \times 5 = 5$

 $5 \times 3 = 15$

The figures in the margin indicate full marks. All symbols are of usual significance.

GROUP-A

1	Answer	any <i>five</i>	questions	from th	e following:
1.	AllSwei	any jive	questions	nomun	e ionowing.

- (a) Distinguish between primary and secondary data.
- (b) What is ogive?
- (c) What do you mean by mean deviation about mean?
- (d) What is scatter diagram?
- (e) Calculate arithmetic mean of the first *n* natural numbers.
- (f) What is skewness?
- (g) Write the three different types of kurtosis.
- (h) What do you mean by rank?

GROUP-B

- 2. Answer any *three* questions from the following:
 - (a) Prove that all odd order central moments are zero for symmetric distribution.
 - (b) Prove that correlation co-efficient does not depend on the origin or scale of the distribution.
 - (c) The means and sds of two samples of sizes n_1 and n_2 are \overline{x}_1 , \overline{x}_2 and s_1 , s_2 respectively. Show that the sd of the composite sample is given by

$$s^{2} = \frac{n_{1}s_{1}^{2} + n_{2}s_{2}^{2}}{n_{1} + n_{2}} + \frac{n_{1}n_{2}(\bar{x}_{1} - \bar{x}_{2})^{2}}{(n_{1} + n_{2})^{2}}$$

- (d) Prove that $\frac{m_4}{m_2^2} \ge \frac{m_3^2}{m_2^3}$, where the symbols have their usual meanings.
- (e) Prove that the correlation coefficient is the geometric mean of the two regression co-efficients.

GROUP-C

- 3. Answer any *two* questions from the following:
 - (a) What do you mean by regression coefficients of y on x? Prove that the angle θ between the two regression lines is given by

$$\theta = \tan^{-1} \left(\frac{1 - r^2}{r} \cdot \frac{s_x s_y}{s_x^2 + s_y^2} \right)$$

where the symbols have their usual meanings.

- (b) What is *r*th order moment about an arbitrary origin *A*? Establish the relation between central and raw moments. Write the expressions for the first four central moments in terms of raw moments.
- (c) The two regression equations are 8x 10y + 66 = 0 and 40x 18y = 214. Also sd of x is 3. Find (i) the average value of x and y. (ii) correlation coefficient between two variables (iii) sd of y.

(d) What do you mean by rank correlation? Prove that $R = 1 - \frac{6\sum d^2}{n(n^2 - 1)}$, where the

symbols have their usual meanings.

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